

1 Article

# 2 **Comminution Effects on Mineral Grade Distribution:** 3 **The Case of an MVT Lead-Zinc Ore Deposit**

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10 **Abstract:** Every mining operation is followed by a beneficiation process aimed at delivering quality  
11 material to the transformation industry. Mainly, in order to obtain valuable minerals from gangue  
12 in mineral processing, comminution and grinding of extracted ore are crucial operations for the  
13 following separation steps. Comminution is the most energy consuming phase, and the quality of  
14 the results is strictly related to the characteristic of the material under treatment. A preliminary  
15 study has been performed in order to understand the crushing behavior of a mixed Zn-Pb sulfide  
16 ore and the distribution of the two target minerals among the products of the process. Ore samples  
17 have been examined and characterized through thin section observation and SEM analyses for the  
18 determination of dimensional grain features, while X-ray powder diffraction (XRPD) quantitative  
19 analyses have been performed for the definition of the concentrations. The selected crushing circuit  
20 comprises lab-scale equipment. For each stage of the process, products below the free-grain size  
21 threshold have been collected, and particle size analyses have been carried out. Comminution  
22 products have been divided in dimensional classes suitable for flotation separation, and XRPD  
23 analyses showed a mineral grade distribution varying with dimension of the products. This  
24 important trend should be considered for further investigation related to an efficient separation.

25 **Keywords:** comminution; mineral processing; mixed sulfides; sphalerite; galena;

26

## 27 **1. Introduction**

28 The mining industry is deeply characterized by essential operations for a proper transformation  
29 process of raw materials into final products. Generally, the exploitation activity in a mine is followed  
30 by a beneficiation process designed to increase the quality of the valuable minerals naturally present  
31 in the excavated material. The very early stage of the transformation is represented by comminution  
32 and grinding of extracted ore aimed at obtaining different changes in terms of dimension and shape  
33 of the material that will be further treated [1,2,3]. Progressively, separation processes are set up in  
34 order to collect and divide target minerals from gangue and waste.

35 Comminution is a highly energy consuming operation, and it is characterized by very low  
36 efficiency [1,4,5,6] and the quality of the final product being strictly related to physical characteristics  
37 of the material under treatment [7,8].

38 The principal objective of comminution is the realization of mineral liberation, that could be not  
39 an easy and predictable outcome but is relevant for an efficient configuration and control of the entire  
40 process, especially when the ore has to be delivered to a flotation process [9,10, 11,12,13]. Shape,  
41 dimension and distribution of free minerals also play a strategic role for the achievement of an  
42 effective beneficiation [14,15].

43 In this study, the crushing behavior of mixed Pb-Zn sulfide ore, mainly containing galena and  
44 sphalerite as valuable minerals, has been analyzed. The separation of these two minerals, usually  
45 performed by froth flotation, is highly affected by comminution and grinding stages [16,17,18].

46 The distribution of concentration of target minerals among the different sized products of the  
47 crushing process has been the key focus of this work. All the evaluations brought a clearer overview  
48 of how different minerals react to the same comminution pathway.

49 The importance of having a clear comprehension of the redistribution of target minerals in mid-  
50 processing products could lead to an efficient separation. Benefits that could be achieved can enhance  
51 a reduction in end-process waste, as well as control of water use, reagents and machinery utilization  
52 during the beneficiation stage.

## 53 2. Materials and Methods

### 54 2.1 Sampling

55 The mixed Pb-Zn sulfide ore samples come from the Val Vedra mine in the Gorno mining  
56 district, Lombardy, Northern Italy. The deposit can be geologically defined as Mississippi Valley  
57 Type (MVT), as described in detail by other authors [19], characterized by a mixed sulfide  
58 mineralization in a carbonate matrix. About 30 kg of material has been collected during the sampling  
59 campaign in order to have a representative set to be studied.

### 60 2.2 Characterization Methods for Samples and Products

#### 61 2.2.1 Optical Microscopy

62 Optical microscopy (OM) was performed on polished thin sections using a *Leica* optical  
63 polarized-light microscope equipped with a *DeltaPix* camera and interfaced with *DeltaPix* software  
64 for image acquisition and processing. This was carried out using normal and polarized transmitted  
65 light on polished thin sections for the determination of the main features of the mineralization and  
66 the average grain size of the target minerals.

#### 67 2.2.2 Scanning Electron Microscopy

68 Scanning electron microscopy (SEM) analyses have been performed using a *FEI Inspect S*  
69 microscope equipped with an EDAX detector and interfaced with *xT Microscope Control* and *GENESIS*  
70 *XM2i* software. The measurement settings were high vacuum mode, 5.00 kV HV and backscattered  
71 electron detector (BSED). Analyses have been performed on uncovered 30 µm thin sections obtained  
72 from rock samples.

#### 73 2.2.3 X-Ray Powder Diffraction Analysis (XRPD)

74 X-ray powder diffraction (XRPD) analysis was performed using a *Rigaku SmartLab SE*  
75 diffractometer, with CuK $\alpha$  radiation at 40kV and 30mA, 5–90° 2 $\theta$  range, 0.01° step width, 1°/min scan  
76 speed equipped with a D/teX Ultra 250 (H) and interfaced with the *SmartLab Studio II* software package.  
77 Quantitative phase analyses have been performed by the whole-powder-pattern fitting (WPPF)  
78 Rietveld method [20–22] as implemented in the software. A pseudo-Voigt peak shape function has  
79 been selected. The refined parameters have been phase scale factor, peak shape parameters, lattice  
80 parameters, preferred orientation and structure coefficients. The ICCD PDF-4 2020 database [23] has  
81 been used for phase recognition and refining.

### 82 2.3 Comminution Flowsheet

83 Physical treatments have been carried out in order to simulate, on a lab-scale, a possible  
84 comminution circuit arrangement for this kind of ore, taking into account the necessity of the material  
85 to be subsequently processed by flotation for an efficient separation of the valuable phases.

86 Figure 1 shows the comminution flowsheet that has been selected in order to test the response  
 87 of the material to different machines. The aim was to produce material with dimensions smaller than  
 88 0.425 mm. Each machine output has been screened at 0.425 mm in order to eliminate the finer part  
 89 and avoid regrinding of ultrafine particles.

### 90 2.3.1 Impact Crusher

91 A *Hazemag* impact crusher has been used as the first primary crusher. This machine has a  
 92 four-lug-bolt rotor, powered by an electrical motor. The feeding opening is 120×120 mm.

### 93 2.3.2 Jaw Crusher

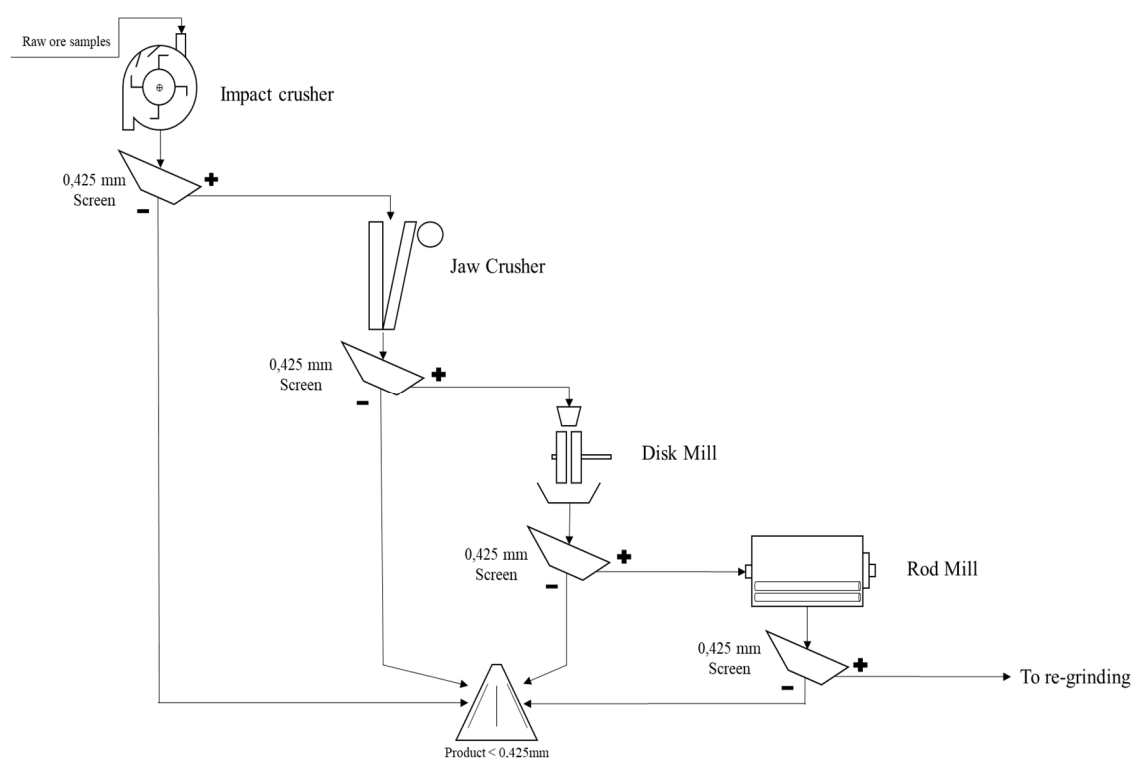
94 A *Magutt-10* jaw crusher has been used for the second phase of the primary crushing. It is  
 95 powered by a 0.75 kW electric engine, at 250 rpm. The selected gap was 5 mm, obtaining a reduction  
 96 ratio equal to 10.

### 97 2.3.3 Disk Mill

98 A *S.I.M.A. Milano* disk mill has been used as first phase for the secondary crushing. The disk gap  
 99 selected was 1 mm, obtaining a reduction ratio of 10 at the output.

### 100 2.3.4 Rod Mill

101 A lab-scale rod mill has been used as the final stage of secondary crushing. It is equipped with  
 102 a 193 mm diameter, 267 mm long drum, containing nine steel rods with a diameter of 8 mm inside,  
 103 powered by a 0.4 kW electrical engine. The drum has been filled with 1 kg of material at 30% v/v  
 104 filling ratio. The grinding time has been 4 min.



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Figure 1. Lab-scale comminution scheme and flowsheet.

## 107 2.4 Sieve Analysis

108 Sizing of material has been performed using different combinations of sieves in dry and wet  
109 conditions, in order to know the size distribution of the comminution output material. Dry sieving  
110 has been selected for general output from each crushing and comminution step. A portion of material  
111 was collected and screened by means of nested screens in decreasing size from the top screen to 0.125–  
112 0.075 mm depending on the fineness of the material and shaken for 3 min in the lab screen shaker.

113 The purpose of wet sieving was, instead, the understanding of granulometric distribution for all  
114 comminution products below 0.425 mm. The sieve sequence consisted of 0.425, 0.355, 0.300, 0.25,  
115 0.212, 0.180, 0.125, 0.090, and 0.063 millimeters, and the screening has been conducted using water as  
116 slime-transporting media, especially for ultrafine particle trapping.

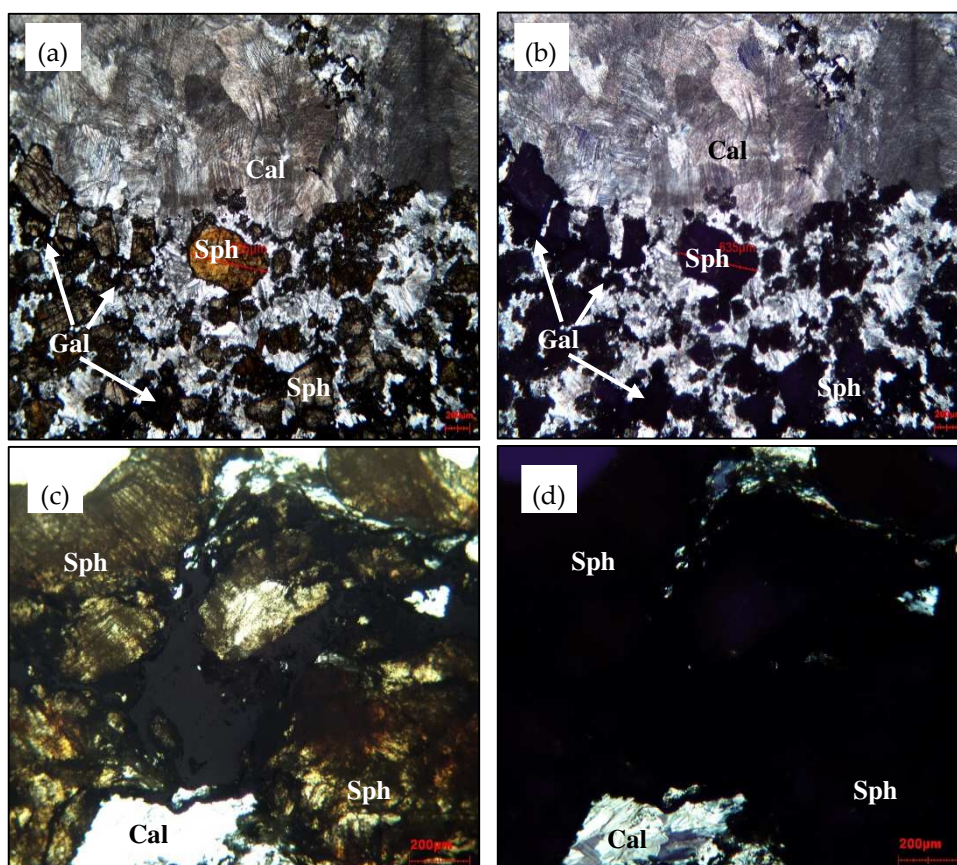
## 117 3. Results

### 118 3.1 Optical Microscopy

119 Observation of thin sections, shown in Figure 2, has been carried out with OM in parallel  
120 transmitted light (PL) and cross-polarized transmitted light (XPL), with objectives between 4× and  
121 10×. There is an abundant presence of sphalerite minerals surrounded by a calcite matrix. Light-  
122 opaque mineralization, such as galena and its altered compounds, have been found. It is possible to  
123 spot some opaque veins, filled with black organic material.

124 Sphalerite grains are massively present in the samples, showing a yellow-brownish and black  
125 coloration, transparent in PL and opaque in XPL. Calcite appears as a white and striated matrix,  
126 transparent both in PL and XPL. Opaque minerals, like galena and cerussite, are sparse and usually  
127 occurring in the surroundings of sphalerite grains

128 Free-grain size, ranging between 0.400 and 0.425 mm, has been defined thanks to digital  
129 measurement from OM images.

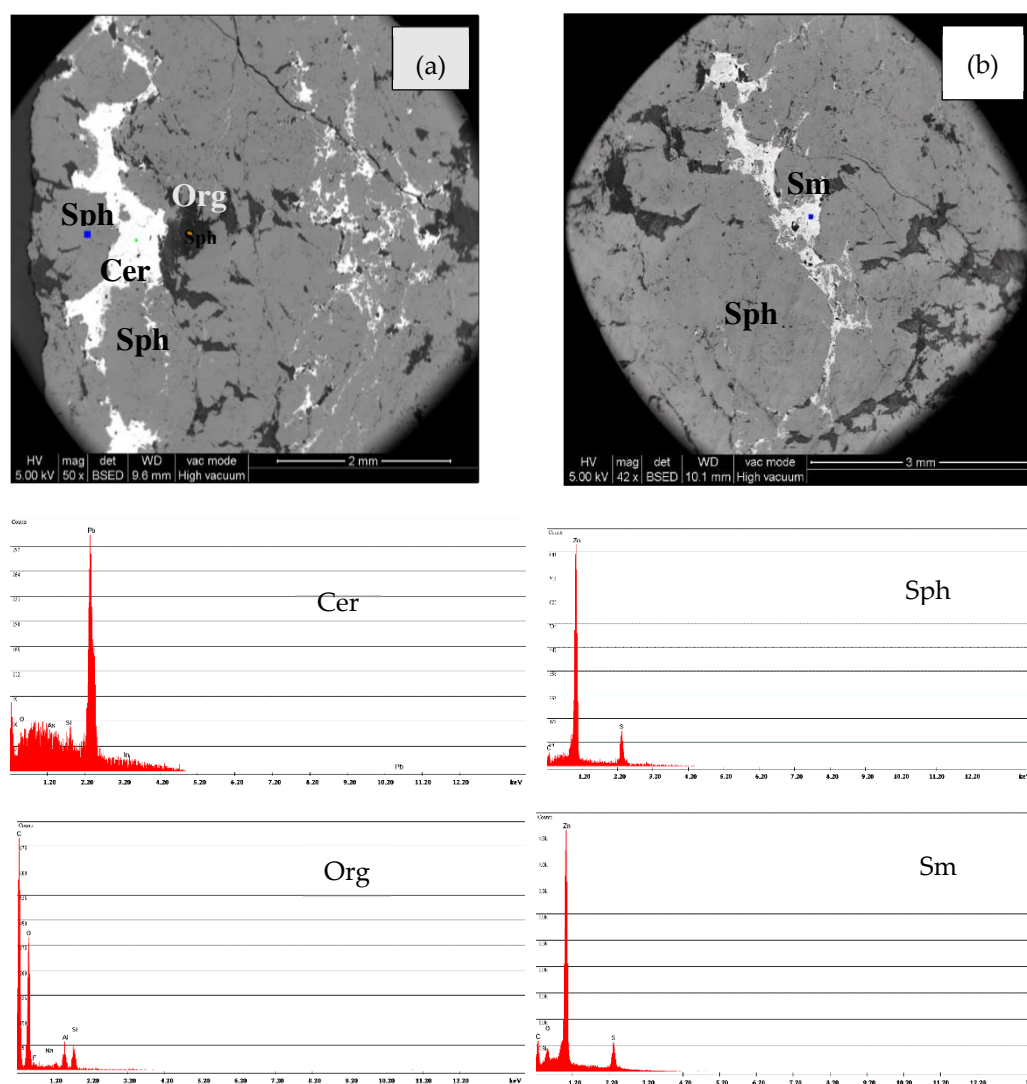


131 **Figure 2.** OM thin sections images in PL and XPL (Sphalerite, *Sph*; Calcite, *Cal*; Galena, *Gal*): (a) Thin  
 132 section n.1, PL and (b) XPL; (c) Thin section n.3, PL and (d) XPL.

### 133 3.2 Scanning Electron Microscopy

134 In order to have elemental information related to the mineralization nature, SEM punctual  
 135 analyses have been performed. The investigation targeted those areas difficult to be characterized by  
 136 OM and the intergranular filled voids present.

137 SEM images and EDS spectra, shown in Figure 3, confirmed a widespread presence of sphalerite  
 138 [24] in the calcite [25] matrix and highlighted the presence of Zn and Pb alteration compounds, mainly  
 139 cerussite [26], anglesite [27] and smithsonite [28]. The presence of organic matter in the microfractures  
 140 has been detected [29].



141 **Figure 3.** SEM images and spectra of thin sections: (a) sphalerite (Sph, blue dot), cerussite (Cer, green  
 142 dot), organic matter (Org, orange dot); (b) sphalerite (Sph) and smithsonite (Sm, blue dot)

### 144 3.3 Comminution

145 The selected flowsheet can be considered as an all-encompassing crushing-comminution  
 146 process, according to [30,31]. Material enters with maximum size of 250 mm and it is reduced to  
 147 millimetric and sub-millimetric grains. The purpose of this test was to bring most of the material  
 148 below the free-grain size, limiting fine and ultrafine fractions that could negatively affect flotation

149 separation [32,33,34,35]. After a preliminary manual reduction performed with a 5 kg hammer, the  
 150 process can be divided in two phases [1]:

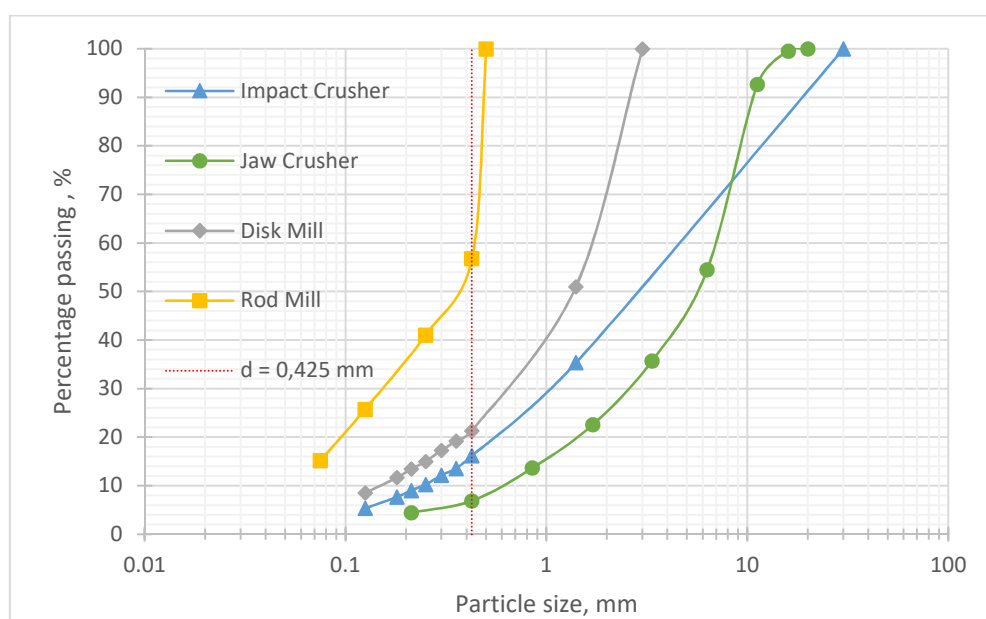
- 151     • primary crushing, with impact crusher and jaw crusher;  
 152     • secondary crushing, with disk mill and rod mill.

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154 Each equipment output has been studied for granulometric assessments and reduction ratio  
 155 checks. Granulometric curves for output material are shown in Figure 4.

156 As plotted in Figure 5, the impact crusher, selected as the first step of the comminution flowsheet,  
 157 resulted in a dimension reduction with contained fine production  $<0.425$  mm of 16.2%wt. The jaw  
 158 crusher, chosen for the second step of primary crushing, gave a lower production of fines. In fact,  
 159 only 6.9%wt. of  $<0.425$  mm has been obtained. At the end of the primary crushing phase, the overall  
 160 fraction having dimension below free-grain size is the 22%wt. of the input material, while the  
 161 overpassing material sent to secondary crushing phases is the 78%wt. In general, primary crushing  
 162 has been successful in minimizing the fine fraction production and reducing the overall size in a  
 163 controlled way.

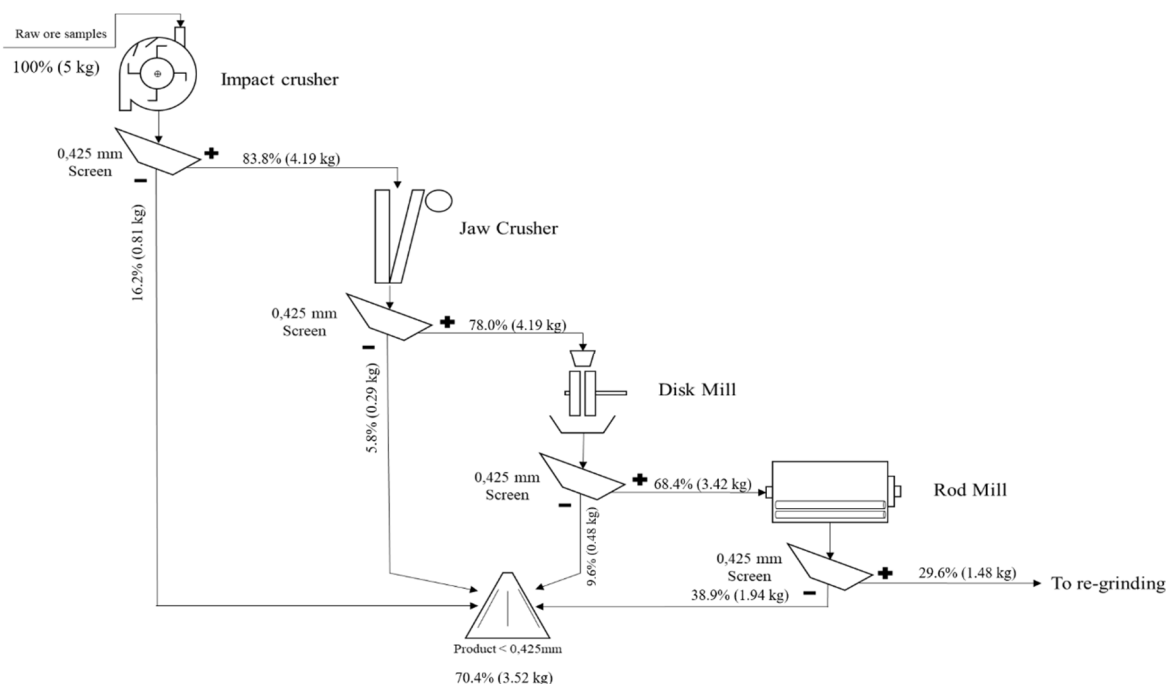
164 For further size reduction, a disk mill has been selected as the first stage of milling. It resulted in  
 165 a material characterized by  $d_{50} > 1.4$  mm, with the fraction of fines being 12.3%wt. The output  
 166 material is homogeneously sized. A rod mill has been the final step of the circuit. It was selected  
 167 aiming to a drastic reduction of the material below the free-grain size of 0.425 mm. Results show how  
 168 4 min of grinding time produced 56.8%wt. of under-passing material. At the end of secondary  
 169 crushing tests, material having  $d < 0.425$  mm is 62.1%wt. of the feed material obtained by primary  
 170 crushing.



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**Figure 4.** Output product granulometric curves for each equipment.

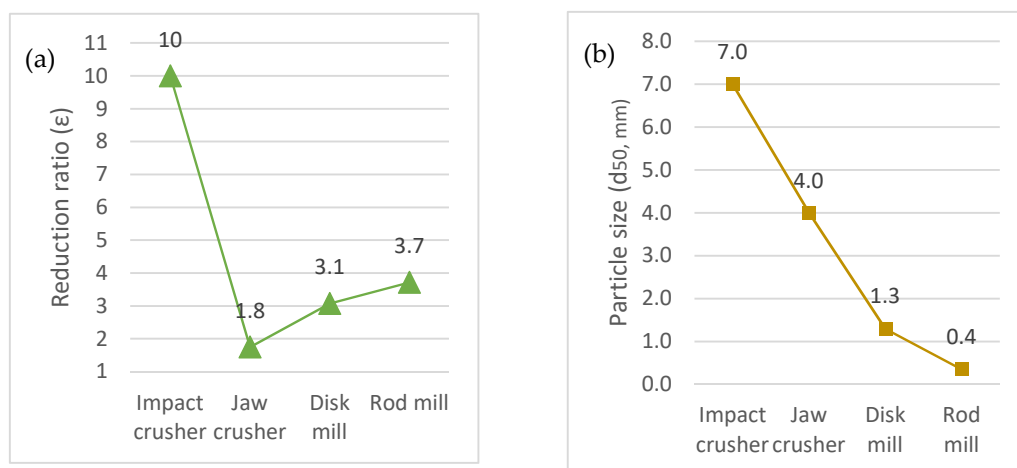


173  
174 **Figure 5.** Comminution flowsheet with input and output mass balance.

175 Reduction ratios of each comminution step have been computed in order to assess the  
176 performances of the circuit. The reduction ratio  $\varepsilon$  is calculated by Eq. 1, with  $d_{50}$  being 50% of the  
177 cumulative weight of the particle size distribution [36]:

178 
$$\varepsilon = \frac{d_{50,Feed}}{d_{50,Product}} \quad (1)$$

179 Figure 6 shows how reduction ratios change among the different equipment considered in the  
180 test. A reduction  $\varepsilon = 10$  for the impact hammer follows a relevant reduction in dimension of material,  
181 as usual for primary crushing [31]. The jaw crusher outputs' reduction ratio drops to  $\varepsilon = 1.8$  due to a  
182 very low production of fines. For the milling phase, the disk mill and rod mill show slightly increasing  
183  $\varepsilon$  values of 3.1 and 3.7, respectively. Overall, the reduction ratios show that the most impacting step  
184 on the size decrease of the material is primary crushing. Secondary crushing is characterized by  $\varepsilon$   
185 smaller than common practice comminution performances [31].



**Figure 6.** Performance parameter for comminution and product dimensions: (a) Reduction ratio trend related to equipment; (b) Change of  $d_{50}$  among comminution products

Overpassing material, accounting for about 30%, has not been reintroduced in any grinding stage, as the overall flowsheet has been arranged as an open-like comminution circuit [1]. All under-passing materials have been collected together and further analyzed as ground product.

### 3.4 Product Sizing

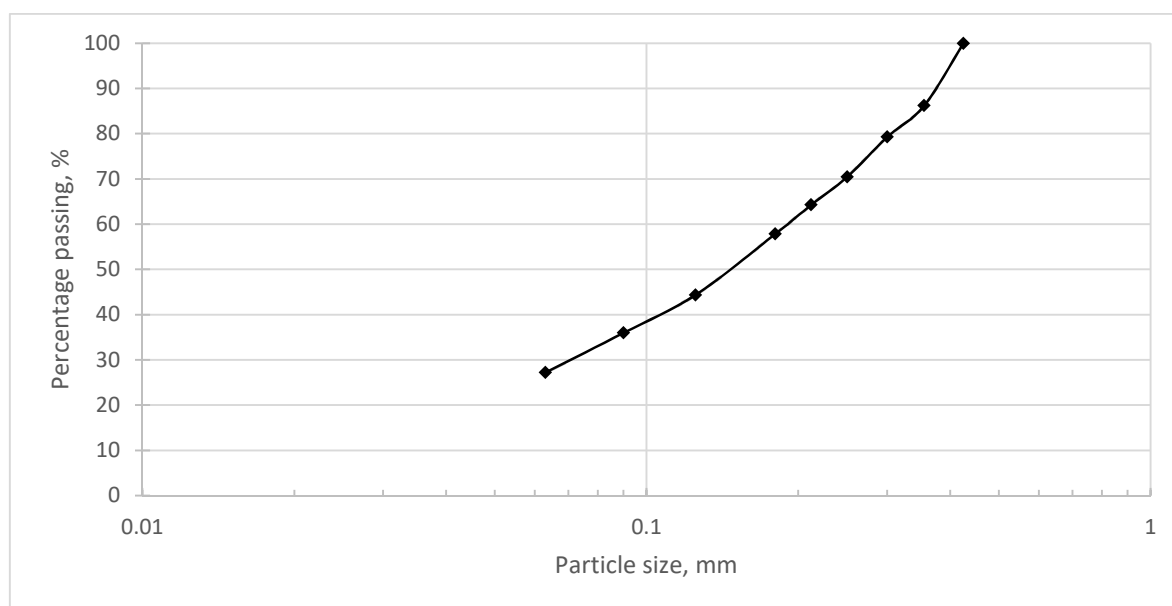
Comminution products passing the 0.425 mm threshold have been more specifically analyzed in terms of granulometric distribution in order to better understand the presence of fine and ultrafine particles. This has been necessary for the assessment of the comminution behavior of the ore, aiming to deliver a good quality material for further separation steps.

Wet sieving methodology has been selected. In Table 1, mesh size and retained and passing material is shown.

**Table 1.** Retained fractions and passing percentage resulting from wet sieving.

Mesh size (mm)	Retained weight fraction (%)	Percentage passing (%)
0.425	0	100
0.350	13.8	86.2
0.300	6.9	79.3
0.250	8.8	70.5
0.212	6.2	64.3
0.180	6.4	57.9
0.125	13.5	44.4
0.090	8.4	36.0
0.063	8.8	27.2
-0.063	27.2	---





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**Figure 7.** Granulometric curve obtained by means of wet sieving on comminution products <0.425 mm

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Figure 7 shows the granulometric curve which has been obtained from previous data, resulting in values of  $d_{80} = 0.300$  mm and  $d_{50} = 0.160$  mm. These findings show that the presence of very fine fractions is relevant. In fact, material below 0.063 mm is 27.2%wt. of the total considered sample. This behavior can be explained by the natural texture of the ore and the mechanical properties of the minerals contained.

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### 3.5 X-Ray Powder Diffraction Analyses

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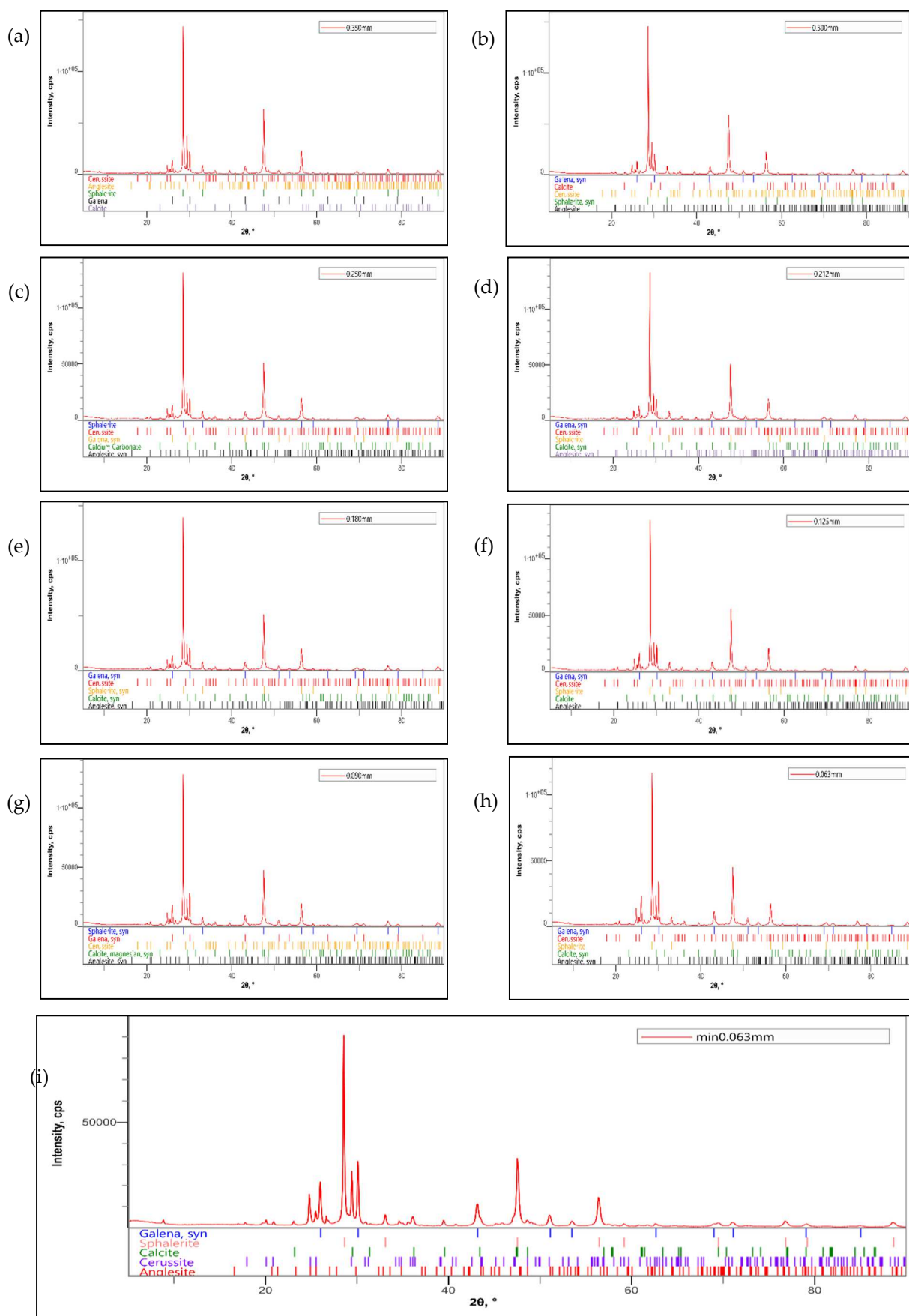
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XRPD analyses, performed on each dimension class obtained by wet sieving, distinguished five different mineral phases: sphalerite, galena, calcite, anglesite, and cerussite as reported in Figure 7. Sphalerite's main peaks has been observed at  $2\theta$  angles of  $28.57^\circ$ ,  $33.11^\circ$ ,  $47.57^\circ$ ,  $56.39^\circ$ ,  $76.77^\circ$  and  $88.52^\circ$  [37]. Calcite's representative peaks have been observed at  $2\theta$  angles of  $29.44^\circ$  and  $48.58^\circ$  [38]. Galena's peaks have been observed at  $2\theta$  angles of  $26^\circ$ ,  $30.09^\circ$ ,  $43.06^\circ$ , and  $50.98^\circ$  [39]. Cerussite's and Anglesite's characteristic peaks have been observed at  $2\theta$  angles of  $24.80^\circ$ ,  $25.49^\circ$ ,  $43.48^\circ$  and  $20.84^\circ$ ,  $23.36^\circ$ ,  $26.75^\circ$  respectively [40,41].

Qualitatively, each class showed a constant presence in terms of mineral phases. Reference spectra [37-41, 23] have been compared with the experimental ones. These outcomes generally confirmed what was previously observed by OM and SEM.



**Figure 8.** XRPD spectra of comminution product sieved classes: (a) 0.425–0.350 mm, (b) 0.350–0.300 mm, (c) 0.300–0.250 mm, (d) 0.250–0.212 mm, (e) 0.212–0.180 mm, (f) 0.180–0.125 mm, (g) 0.125–0.090 mm, (h) 0.090–0.063 mm, (i) <0.063 mm.

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223 Quantitative XRPD analyses obtained by Rietveld [20–22] refinement showed residual errors  $R_{wp}$   
 224 ranging from 5.50% to 6.49% and goodness-of-fit in the range from 2.06 and 2.41 as shown in Table  
 225 2.

226 **Table 2.** Observed residual errors ( $R_{wp}$ ) and goodness-of-fit (S) from quantitative XRPD analysis.

Particle size (mm)	$R_{wp}$ (%)	S
0.425–0.350	5.90	2.20
0.350–0.300	5.54	2.07
0.300–0.250	5.55	2.07
0.250–0.212	5.55	2.06
0.212–0.180	6.21	2.33
0.180–0.125	5.50	2.05
0.125–0.090	5.86	2.20
0.090–0.063	5.87	2.21
<0.063	6.49	2.41

227 According to some authors, a Rietveld refinement showing low  $R_{wp}$  and S values can be  
 228 considered as reliable with errors in weight fraction estimation between 0.5%wt. and 1.5%wt. [42,43].  
 229 Quantitative results are shown in Table 3. On average, sphalerite is the most abundant phase in the  
 230 samples, ranging 50–70%wt., calcite defined as gangue mineral attained 17–27%wt., while galena  
 231 ranges 4–9%wt. Other phases can be considered as minor. The accuracy of the quantitative analyses  
 232 has not been assessed in detail.  
 233

234 **Table 3.** Quantitative XRPD results for each particle size.

Particle size class (mm)	Weight Fraction (%) <sup>(1)</sup>				
	ZnS	PbS	PbCO <sub>3</sub>	PbSO <sub>4</sub>	CaCO <sub>3</sub>
0.425–0.350	65.59	4.09	2.52	2.93	24.87
0.350–0.300	66.82	4.14	3.04	2.67	23.33
0.300–0.250	69.32	4.28	3.08/	2.50	20.82
0.250–0.212	67.35	4.12	3.11	3.55	21.87
0.212–0.180	70.39	4.60	3.71	4.04	17.26
0.180–0.125	68.22	5.37	3.27	2.79	20.35
0.125–0.090	65.88	6.54	3.97	4.10	19.51
0.090–0.063	62.63	8.41	4.94	3.53	20.49
<0.063	51.50	7.97	6.43	7.20	26.90

235 1. Estimation errors must be considered in the range  $\pm 0.5$ –1.5% according to [42,43]

236 Some of the mineral phases present in the samples show a different concentration among  
 237 different granulometric classes. The clearest evidence is the one linked with galena and Pb-related  
 238 compounds. Their total concentration is around 9.5%wt. in particle size 0.425–0.350 mm and reaches  
 239 21.6%wt. in particle size <0.063 mm, constantly increasing their presence with the decrease of material  
 240 dimension. Galena is the most abundant regarding Pb-related compounds and shows a worthwhile  
 241 concentration for further recovery.

242 Sphalerite is the most abundant phase in each size, but its presence decreases from 0.180 mm,  
 243 where it peaks with 70.4%wt., toward finer classes. The lowest concentration of ZnS is 62.6%wt.,  
 244 found in the <0.063 mm class. The calcite phase has its lowest presence in class 0.212–0.180 mm with  
 245 17.3%wt., while its highest concentration of 26.9%wt. is measured in the <0.063 mm class.

246 In general, high values of valuable minerals have been found in the different classes of  
 247 comminution products, underling the necessity of further separation in order to obtain high quality  
 248 concentrates from the ore. In the choice of recovery and separation methods of Pb-related minerals,

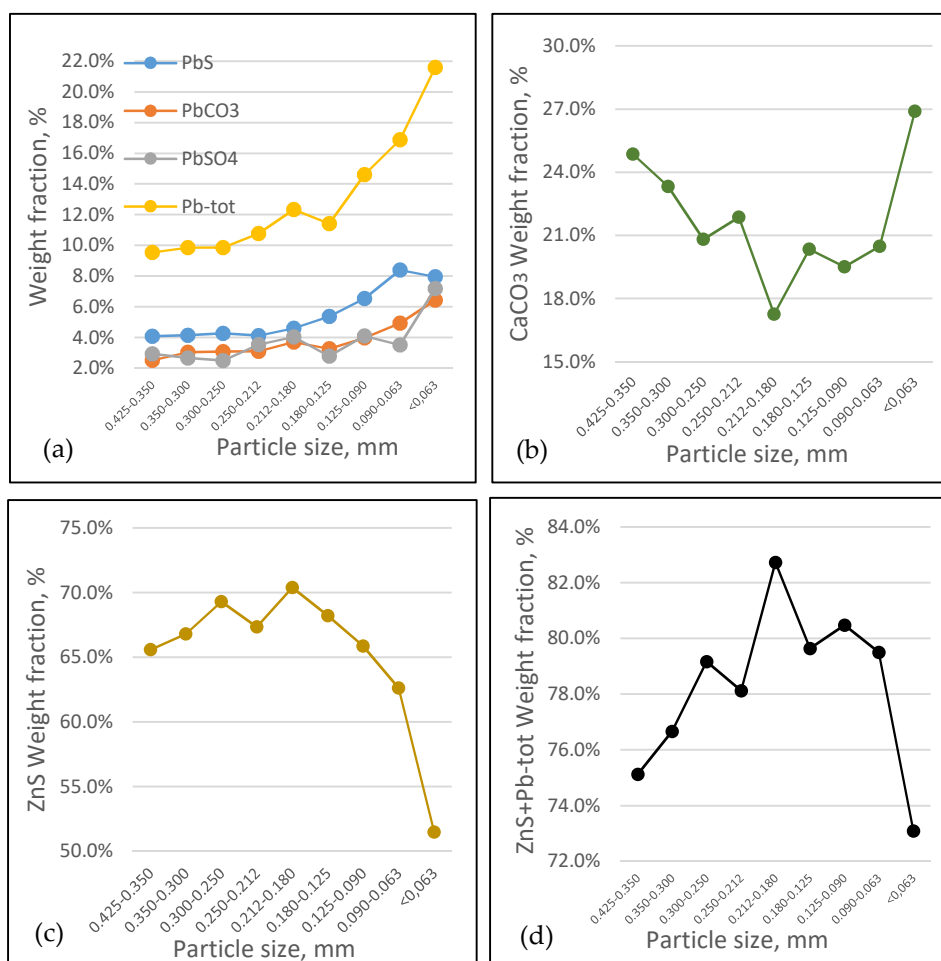
249 galena in particular, the increase of their concentration in the finest classes should be taken in  
250 consideration.

#### 251 4. Discussion

252 The purpose of this study was to understand the distribution of target minerals among mineral  
253 processing products, particularly after a lab-scale comminution test. In order to have an overview of  
254 the characteristics of the sampled ore, petrographic observations have been necessary for the  
255 determination of the shape, composition and dimension of grains present in the mineralized mixed  
256 sulfide ore collected in an MVT deposit in Northern Italy. As described above, thin sections have  
257 been realized and observed. Results showed typical characteristics related to MVT deposits [19,44],  
258 with relatively high content of sphalerite minerals embedded in a calcite matrix. Galena is sparsely  
259 present in very small crystals, difficult to be distinguished only by OM.

260 SEM characterization brought additional information, especially concerning alteration products  
261 and filling of the ore's microfractures. The presence of cerussite, anglesite and organic matter has  
262 been detected, confirming the presence of Pb-related minerals and traces of organic matter, arguably  
263 linked with the formational geological environment of the site [19]. The observation made on the  
264 dimensional characteristics resulted in an estimated liberation size of valuable minerals ranging  
265 between 0.400 and 0.450 mm. On these parameters, a lab-scale comminution open circuit has been  
266 arranged, with the rod mill being the phase that mostly controls the final output products. A 30%wt.  
267 of the initial input material needs to be reground and has not been considered (Figure 5). Ground  
268 product contains 27%wt. of material <0.063 mm (Table 1).

269 XRPD quantitative analyses highlighted the important presence of sphalerite and galena in  
270 dimension classes ranging between the 0.250 and 0.063 mm classes, as shown in Figure 8a and Figure  
271 8d. This size range is considered suitable for separation processes such as froth flotation or  
272 gravimetric methods [1,45,46]. Concerning the presence of Pb-related compounds in very fine classes,  
273 a non-conventional flotation [47,48] should be tested. Target phase concentration has been observed  
274 as fluctuating, varying with the reduction in dimension of products (Figure 9). This phenomenon  
275 could be framed in a selective comminution behavior of the ore [36], but in this study further data  
276 should be collected in order to better define parameters related to this specific possibility.



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**Figure 9.** Mineral phases weight fraction variation among dimension classes in comminution products below 0.425 mm: (a) Pb-related compounds, (b) calcite, (c) sphalerite, (d) valuable phases assumed as sum of sphalerite and Pb-related compounds.

281 The calcite trend appears as V-shaped, encountering a descending behavior until the 0.212–0.180  
282 mm class, strictly related to total valuable phase ZnS + Pb-tot peak.

283 Considering the sum of ZnS and Pb-related, plotted in Figure 9d and corresponding to the  
284 valuable minerals present in the ore, their trend is mainly dominated by sphalerite oscillations in the  
285 samples (Figure 9c). Peak concentration is reached in the 0.212–0.180 mm class with 82.7%wt., while  
286 their lowest occurrence of 73.1%wt. is in the <0.063 mm particle size, as shown in Figure 9d.

287 Moreover, thanks to quantitative analyses, important information has been obtained for the  
288 evaluation of the most suitable dimension classes to be delivered to following separation stages. This  
289 important trend should be considered for further studies related to the mineral recovery rate  
290 achievable by froth flotation. Generally, the amount of valuable mineral phases is relevant and  
291 worthwhile. Further detailed studies should be taken into consideration.

292

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298 Writing—Review and Editing, G.B., O.B. and P.M.; Supervision, P.M.

299 **Conflicts of Interest:** The authors declare no conflict of interest.

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